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## THE EMBODIMENTS OF THE INVENTION IN WHICH AN EXCLUSIVE PROPERTY OR PRIVILEGE IS CLAIMED ARE DEFINED AS FOLLOWS:

- A method for determining a result of a group operation performed an integral
   number of times on a selected element of the group, said method comprising the steps of
  - (a) representing said integral number as a binary vector;
  - (b) initializing an intermediate element to the group identity element;
  - (c) selecting successive bits, beginning with a left most bit, of said vector and for each of said selected bits;
    - (i) performing said group operation on said intermediate element to derive a new intermediate element;
    - (ii) replacing said intermediate element with said new intermediate element;
    - (iii) performing said group operation on said intermediate element and an element, selected from the group consisting of:

      said group element if said selected bit is a one; and an inverse element of said group element if said selected bit is a zero;
    - (iv) replacing said intermediate element with said new intermediate element;
  - (d) performing said group operation on said intermediate value and said inverse element if said last selected bit is a zero; and replacing said intermediate element therewith, to obtain said result, whereby each of the bits of said integral is processed with substantially equal operations thereby minimizing timing attacks on said cryptographic system.
- A method as defined in claim 1, said group being a multiplicative group F<sub>p</sub>\* said
   group element being an integer, and said group operation being exponentiation g<sup>a</sup> and an inverse element being the multiplicative inverse 1/g.

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- 3. A method as defined in claim 1, said group being an additive group  $E(F_{2^{\mu}})$  and said group operation being addition of points.
- 4. A method as defined in claim 1, said group being an additive group  $E(F_q)$ , said group element being a point P with coordinates (x,y) on the elliptic curve, and said group operation being the scalar multiple kP of said point and an inverse element being the negative -P of said point.
- 5. A method as defined in claim 1, said integral value being a private key k.
- 6. A method of performing a selected group operation on a scalar and a selected element of said group, in a cryptographic processor, said method comprising the steps of:

representing said scalar as a binary vector;

recoding said binary vector to produce a signed digit representation of plus one and minus one digits;

selecting each of said recoded bits sequentially and for each of said selected bits performing said group operation on an intermediate element to derive a new intermediate element; and adding or subtracting said selected element to said intermediate element in accordance with said sign if said digit being selected; and

outputting said intermediate value as a result of said group operation.